

## 第 6 8 回 広島数理解析セミナー ( 2 0 0 3 年度 )

### Hiroshima Mathematical Analysis Seminar No.68

日時 : 1 2 月 1 2 日 ( 金 ) 1 5 : 0 0 ~ 1 6 : 0 0

場所 : 広島大学理学部 B 7 0 7

講師 : Professor Reinier van der Hout ( International University Bremen, Germany )

題目 : Nematic liquid crystals and harmonic maps

要旨 : This work has been motivated by the study of pressure-driven flow of a nematic liquid crystal (n.l.c.) through a long circular cylinder.

A nematic liquid crystal is a fluid, equipped with a field  $\mathbf{u}$  of preferred directions (of unit length), with an associated energy density  $e(\mathbf{u}) := k|\nabla\mathbf{u}|^2 = k\Sigma_{i,j} \left(\frac{\partial u_i}{\partial x_j}\right)^2$ . This energy-density establishes a link with *harmonic maps* into the unit sphere  $S^2$ .

We discuss some solved and some open problems for cylindrical flow of an n.l.c.. Then, we discuss the related problem of symmetric harmonic maps  $D^2 \rightarrow S^2$  and their heat flows, with  $D^2$  the unit disk. Especially, we discuss the phenomenon of discrete energy-concentration and the question whether concentrated energy can be recovered; this question is closely related to the non-uniqueness of the heat flow. Finally, we discuss the nonoccurrence of multiple simultaneous energy-concentration events.

Much of this is joint work with Michiel Bertsch, Roberta Dal-Passo and Elisabetta Vilucchi (Roma II).

#### 広島数理解析セミナー幹事

池畠 良 ( 広大教育 ) ikehatar@hiroshima-u.ac.jp

宇佐美広介 ( 広大総科 ) usami@mis.hiroshima-u.ac.jp

大西 勇 ( 広大理 ) isamu\_o@math.sci.hiroshima-u.ac.jp

★川下 美潮 ( 広大理 ) kawasita@math.sci.hiroshima-u.ac.jp

倉 猛 ( 広大理 ) kura@math.sci.hiroshima-u.ac.jp

柴田徹太郎 ( 広大総科 ) shibata@mis.hiroshima-u.ac.jp

滝本 和広 ( 広大理 ) takimoto@math.sci.hiroshima-u.ac.jp

松本 敏隆 ( 広大理 ) mats@math.sci.hiroshima-u.ac.jp

★印は本セミナーの責任者です